

## Joint Probability Distributions - Discrete Case

- (1) A supermarket has two express lines. Let  $X$  and  $Y$  denote the number of customers in the first and in the second, respectively, at any given time. During non-rush hours, the joint pdf of  $X$  and  $Y$  is summarized by the following table:

		X			
		0	1	2	3
Y	0	0.1	0.2	0	0
	1	0.2	0.25	0.05	0
	2	0	0.05	0.05	0.025
	3	0	0	0.025	0.05

Find  $P(|X - Y| = 1)$ , the probability that  $X$  and  $Y$  differ by exactly 1.

- (2) Suppose two fair dice are rolled. Let  $X$  be the sum of the numbers showing, and let  $Y$  be the larger of the two. Find  $p_{X,Y}(2, 3)$ ,  $p_{X,Y}(4, 3)$ , and  $p_{X,Y}(6, 3)$ .

- (3) From a group of three Republicans, two Democrats, and one independent, a committee of two people is to be randomly selected. Let  $X$  denote the number of Republicans and  $Y$  denote the number of Democrats on the committee. Find the joint probability density function of  $X$  and  $Y$  and then find the marginal pdf of  $X$ .