

(1) Determine whether the following matrices are invertible. If invertible, find the inverse.

(a)  $A_1 = \begin{bmatrix} 2 & 3 \\ 1 & 2 \end{bmatrix}$

(b)  $A_2 = \begin{bmatrix} 0 & 2 \\ 3 & 0 \end{bmatrix}$

(c)  $A_3 = \begin{bmatrix} 2 & 0 \\ 4 & 2 \end{bmatrix}$

(d)  $A_4 = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix}$

(e)  $A_5 = \begin{bmatrix} 1 & 3 \\ 2 & -6 \end{bmatrix}$

(f)  $A_6 = \begin{bmatrix} 2 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 2 \end{bmatrix}$

(2) Write the system in matrix form, and then use the inverse of the coefficient matrix to find the solution of the system.

$$2x_1 + 3x_2 = 1$$

$$x_1 + 2x_2 = 5$$

(3) Write the system in matrix form, and then use the inverse of the coefficient matrix to find the solution of the system.

$$2x_1 - x_2 = 1$$

$$-x_1 + 2x_2 - x_3 = 2$$

$$-x_2 + 2x_3 = 3$$