MATH 133 - 01

Worksheet 2

- 1. Find $f \circ g \circ h$.
 - (a) f(x) = x + 1, g(x) = 2x, h(x) = x 1. (b) $f(x) = \sqrt{x - 1}$, $g(x) = x^2$, $h(x) = x^3 + 2$.
- 2. Express the function in the form $f \circ g$.

(a)
$$F(x) = \cos^2 x$$
 (b) $u(t) = \frac{\tan t}{1 + \tan t}$

3. Express the function in the form $f \circ g \circ h$.

(a)
$$H(x) = 1 - 3^{x^2}$$

(b) $R(x) = \sqrt{\sqrt{x} - 1}$
(c) $S(t) = \sin^2(\cos t)$

4. A stone is dropped into a lake, creating a circular ripple that travels outward at a speed of 60 cm/s.

- (a) Express the radius r of this circle as a function of the time t (in seconds).
- (b) If A is the area of this circle as a function of the radius, find $A \circ r$ and interpret it.
- 5. If you invest x dollars at 4% interest compounded annually, then the amount A(x) of the investment after one year is A(x) = 1.04x. Find $A \circ A$, $A \circ A \circ A$, and $A \circ A \circ A \circ A$. What do these compositions represent? Find a formula for the composition of n copies of A.