Let $X, Y$ be random variables. If $m_{X}(t)=m_{Y}(t)$ for all $t$ in an interval, then $X, Y$ have the same distribution.

