

**College of the Holy Cross, Spring Semester, 2019**  
**Math 134 Worksheet 8**  
**Due Tuesday, February 26**

1. Let  $R$  be the region enclosed by the parabolas  $y = x^2 + 1$  and  $y = 3 - x^2$ .
  - (a) Find the area of  $R$ .
  - (b) Find the volume of the solid obtained by revolving  $R$  around the  $x$ -axis.
  - (c) Find the volume of the solid obtained by revolving  $R$  around the line  $y = -2$ .
2. Use integration by parts to evaluate the following integrals.

(a) $\int x^2 e^{7x} dx$	(c) $\int x^2 \sin^{-1}(x) dx$	(e) $\int e^{\sqrt{x}} dx$
(b) $\int \sqrt{x} \ln(x) dx$	(d) $\int e^x \cos(2x) dx$	(f) $\int (\ln(x))^2 dx$

3. Use integration by parts to derive the following reduction formula:

$$\int \cos^n(x) dx = \frac{1}{n} \cos^{n-1}(x) \sin(x) + \frac{n-1}{n} \int \cos^{n-2}(x) dx$$

4. Use the reduction formula above to evaluate  $\int \cos^n(x) dx$  for  $n = 2, 3, 4$ , and  $5$ .
5. Use the formula

$$\int \sec^n u du = \frac{1}{n-1} \tan u \sec^{n-2} u + \frac{n-2}{n-1} \int \sec^{n-2} u du$$

to evaluate  $\int \sec^n(x)$  for  $n = 4$  and  $n = 6$ .

6. Use the formula

$$\int \tan^n u du = \frac{1}{n-1} \tan^{n-1} u - \int \tan^{n-2} u du$$

to evaluate  $\int \tan^n(x)$  for  $n = 3$  and  $n = 4$ .