

MONT 105Q – Mathematical Journeys
Hypothesis Testing Practice Problems
April 1, 2016

Directions:

For each question, first identify and state relevant null and alternative hypotheses. Then carry out the indicated hypothesis test, state your conclusions briefly and cogently, and answer any other questions.

- 1) The average CO_2 emissions for a collection (sample) of 100 large power plants is $\bar{Y} = 2223.1$ lb/Mwh, with sample $SD = 211.3$ lb/Mwh.
 - a) If this were a random sample, and we carried out a hypothesis test designed to make the probability of a Type I error equal $\alpha = .05$, would there be sufficient evidence to say that the average coal-fired power plant emits an amount greater than 2200 lb/Mwh?
 - b) But now, suppose you knew that this data was collected from just the 100 largest power plants in the country. Is this a random sample? Does the calculation in part a) really make sense in this setting?

- 2) In a sample of $n = 50$ field mice caught in the wild, the average body length (excluding the tails) was $\bar{Y} = 6.8$ cm with a sample $SD = .4$ cm. With a hypothesis test designed to make the probability of a Type I error equal $\alpha = .05$, would there be sufficient evidence to say that population body length is different from 7 cm?

- 3) A medical study compared the resting pulse rates of random, independent samples of 100 smokers and 100 nonsmokers. The smokers had an average pulse rate of $\bar{Y} = 86$ beats per minute with $SD_1 = 5.4$, while the nonsmokers had an average pulse rate of $\bar{X} = 80$ and $SD_2 = 4.9$. With a hypothesis test designed to make the probability of a Type I error equal $\alpha = .01$, would there be sufficient evidence to say that nonsmokers have a lower average pulse rate?