## MATH 135 – Calculus 1 Extreme Values November 11, 2019

## Background

Recall from today's video:

- A continuous function on a closed interval attains a *maximum value* and a *minimum value* on that interval.
- Those maximum and minimum values are attained either at endpoints of the interval or at interior points nothing deep going on there, just logic(!)
- If the maximum or minimum value is attained at a point x = c other than an endpoint, then c must be a critical point of f either a solution of f'(c) = 0, or else a place where f'(c) does not exist.
- So to find the maximum and minimum value of a continuous function of a continuous f(x) on a closed interval [a, b], we can:
  - (i) Compute f'(x) and find all critical points c in [a, b].
  - (ii) Compute f(a), f(b), and f(c) for all critical points found in the first step.
  - (iii) Then the maximum value will be the largest of the numbers found in the previous step and the minimum value will be the smallest of those numbers.

## Questions

For each of the following functions,

- (i) determine all critical points in the given interval,
- (ii) compute the values of f at the critical points in the interval, and compute the values at the endpoints of the interval,
- (iii) determine the maximum and minimum values of f on the interval.

This is the process sketched above(!)

1.  $f(x) = x^3 - 12x^2 + 21x$  on [0, 11].

2. 
$$f(x) = (x^2 + 2x)e^{-x}$$
 on [1,5]

- 3.  $f(x) = 5 \tan^{-1}(x) x$  on [-5, 5].
- 4.  $f(x) = (x x^2)^{2/3}$  on [0, 2]. (Note: Careful on this one you should find critical points where f'(x) does not exist.)