

MATH 134 – Calculus with Fundamentals 2  
Practice Days on “Time Value of Money” Concepts  
April 24 and 26, 2018

*Background*

Refer to the formulas on the second sheet as needed.

- (A) Mary deposits \$3000 in an interest-bearing checking account but never writes any checks on it. What will be the balance in the account after 8 years if the nominal annual interest rate is 1.1% and the compounding is done
- (a) monthly
  - (b) continuously
  - (c) daily (*Don't* ignore leap years now. How many of them are there in an 8 year period? Is it always the same number?)
  - (d) What is the effective annual interest rate in each case?
- (B) How much would new parents have to set aside in one lump sum at the birth of a child in order to have \$60000 on hand for the first year tuition bill when the child turns 18 years old and goes off to college? Assume they can realize a return of 7% per year compounded continuously on the investment instrument they choose.
- (C) In the situation of question (B), suppose the parents make payments of \$350 per month into an investment account earning 7% per year every month between the birth of the child and when the child turns 18. How much money will be in the account at that time?
- (D) You are a lender making small business loans.
- (1) A potential customer comes to you and asks for a loan of \$50000 to be repaid by a stream of monthly payments over 4 years. If you *didn't* make the loan you could invest the \$50000 at a 5% annual interest rate for four years. So you need to consider the future value of \$50000 at 5% to think about how to set up the loan. What is that future value?

- (2) How should you set the monthly payment on a loan to make the future value of the income stream consisting of monthly payments over 4 years equal to the future value of the \$50000?
- (3) You write a check for \$50000 to the borrower at the start of the loan and then collect the payments for 4 years. At the end of the four years, how much money have you made on the deal? Be sure to explain how you are thinking about this.