

# Ordinary Differential Equations

MATH 304, MWF 12:00 - 12:50, Swords 302, Fall 2006

Dr. Gareth Roberts

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**Office hours:** Mon. 10 - 11, Tues. 10:30 - 12, Wed. 10 - 11, Fri. 8 - 9 or by appointment.

**Required Text:** *Differential Equations*, Third ed., Paul Blanchard, Robert Devaney and Glen Hall

**Course Prerequisites:** MATH 242 (Principles of Analysis) and MATH 244 (Linear Algebra)

**Web page:** <http://mathcs.holycross.edu/~groberts/Courses/MA304/homepage.html>  
Homework assignments, computer projects, schedule changes, exam materials, useful links and other important information will be posted at this site. Please bookmark it!

**Computer Projects:** There will be several computer projects assigned over the course of the semester using the software package DE Tools included with the course text. Each project will explore some real world application of differential equations and may require some supplementary reading. Projects will be completed in groups of 2 to 3 people with one report to be turned in for the entire group.

**Syllabus:** This is an applied mathematics course focusing on ordinary differential equations, that is, equations relating the derivatives of unknown functions to themselves. For example, the differential equation  $dy/dt = 2y^2 - y$  relates the derivative of the unknown function  $y(t)$  to a quadratic expression of the function itself  $2y(t)^2 - y(t)$ . Another example, well-known to engineering students, is the equation for a damped harmonic oscillator with external forcing:

$$m \frac{d^2y}{dt^2} + b \frac{dy}{dt} + ky = a \cos(\omega t)$$

Here, the unknown function  $y(t)$  represents the position of a mass  $m$  at time  $t$  attached to a mounted spring. There are literally thousands of differential equations used to model phenomena in all kinds of fields including physics (mechanics), chemistry (reactions), biology (population models), neuroscience (brain functioning), economics, astronomy (space craft trajectories) and fluid dynamics (turbulence). Any natural process that involves a change over time can be modeled with a differential equation.

We will utilize three different approaches to studying differential equations: analytic, numerical and qualitative techniques. Since most differential equations are too large in dimension or too difficult to solve explicitly, qualitative methods play an important role in modern research. With the rapid growth in technology, using computers to approximate and visualize solutions has also become increasingly common. In order for you to obtain an appreciation for this aspect of the field, several computer projects using the software package DE Tools (included with the course text) will be assigned.

We will cover most of the material from Chapters 1 through 5 and then finish with a brief tour of one of my favorite subjects, celestial mechanics. Other topics such as Picard iteration, the Poincaré map and dynamical systems theory will be covered if time permits. A rough outline of the semester is as follows:

- First-Order Equations: population models, separation of variables, slope fields, Euler's method (5 classes)
- First-Order Equations: existence and uniqueness theorems, phase lines, bifurcations, solving linear equations (7 classes)
- Exam I
- Systems: physical examples, vector fields, Euler's method, the Lorenz equations (5 classes)
- Planar Linear Systems: eigenvalues and eigenvectors, analytic solutions, sketching phase planes, the trace-determinant plane (7 classes)
- The Harmonic Oscillator: 2nd-order equations, forced oscillators, resonance (4 classes)
- Exam II
- Nonlinear Systems: equilibria, stability, nullclines, Hamiltonian systems (5 classes)
- Celestial Mechanics: the Kepler problem, the  $n$ -body problem, special solutions (4 classes)
- Final Exam

**Homework:** There will be homework due every Wednesday at the START of class. Assignments will be posted on the course web page. There will be a list of problems for you to hand in, a nonempty subset of which will be graded. While you are allowed and encouraged to work on homework problems with your classmates, the solutions you turn in to be graded should be your own. Take care to write up solutions **in your own words**. Plagiarism will not be tolerated and will be treated as a violation of both the departmental policy on academic integrity and the college's policy on academic honesty.

**NOTE:** LATE homework will NOT be accepted. The only excused homework which is late will be accompanied by a letter from your Class Dean. However, you will be allowed ONE "mulligan" over the course of the semester where you can turn in the assignment up to one week after the original due date.

**Exams:** There will be two evening midterms and a comprehensive final at the end of the semester. Please make a note of these dates and plan accordingly. Any conflicts must be legitimate and brought to my attention well before the scheduled exam date. If you have any specific learning disabilities or special needs and require accommodations, please let me know early in the semester so that your learning needs may be appropriately met. You will need to contact the director of Disability Services in Hogan 209 (x 3693) to obtain documentation of your disability. We will review for the midterms during the Monday class on the week of the exam.

	<b>Exam 1</b>	<b>Wed., Oct. 4</b>	<b>6:00 - 7:30 pm</b>
<b>Exam Schedule:</b>	<b>Exam 2</b>	<b>Wed., Nov. 15</b>	<b>6:00 - 7:30 pm</b>
	<b>Final</b>	<b>Sat., Dec. 16</b>	<b>2:30 - 5:30 pm</b>

**Academic Integrity:** The Department of Mathematics and Computer Science has drafted a policy on academic integrity to precisely state our expectations of both students and faculty with regards to cheating, plagiarism, academic honesty, etc. You are required to read this policy and sign a pledge agreeing to uphold it. Anyone who violates the Departmental Policy on Academic Integrity will receive a 0 for that assignment as well as possible further disciplinary action involving your Class Dean.

**Grade:** Your course grade will be determined as follows: homework 25%, computer projects 20%, midterm exams 30% and final exam 25%.

**How to do well in this course:**

- Attend class, participate and ask questions.
- Work with your classmates. Organize study groups.
- Be an active, aggressive learner.
- Do your homework regularly.
- Read the text. (It even has a few jokes!)

*Never regard study as a duty, but as the enviable opportunity to learn.*

Albert Einstein