

# Math 132: Calculus for the Physical & Life Sciences 2

Spring 2006

## Practice Questions for Midterm 1

1. Compute the following:

(a)  $\int 2x(x^2 + 5)^{7/2} dx$

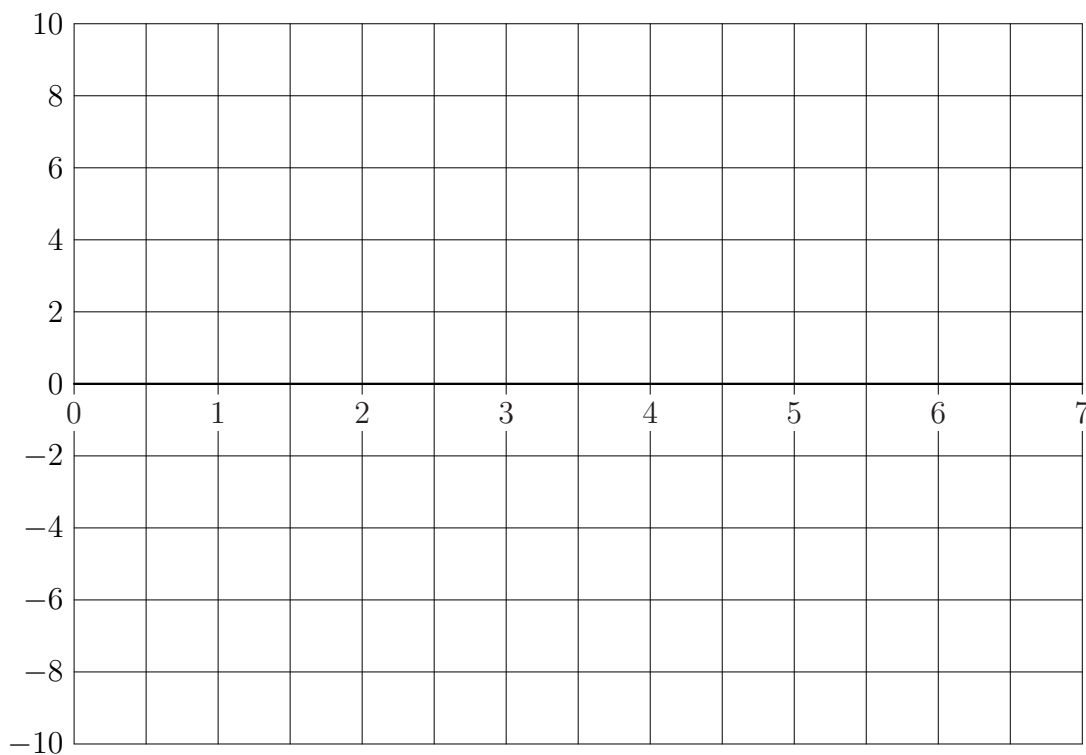
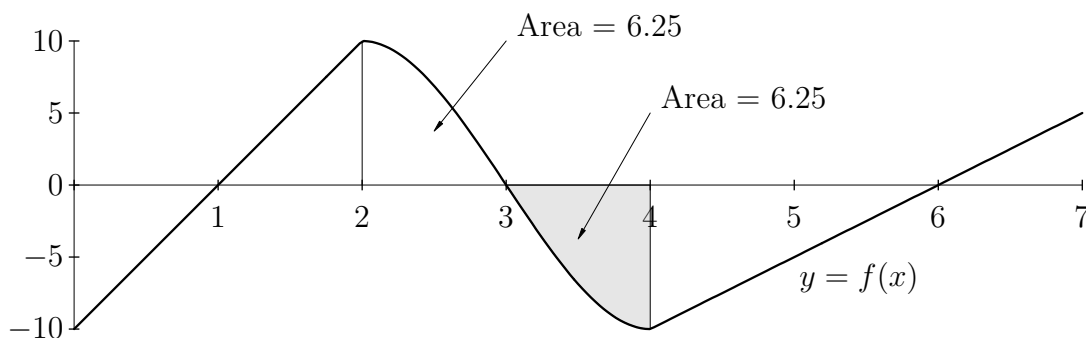
(b)  $\int \sin(3\theta) d\theta$

(c)  $\int \frac{dx}{2x + 1}$

(d)  $F'(x)$ , where  $F(x) = \int_{\pi}^x \frac{t}{1 + \sin^2 t} dt$

2. The graph  $y = f(x)$  is shown. Let  $F$  be the antiderivative of  $f$  satisfying  $F(2) = 0$ . Find the indicated values, and carefully sketch the graph  $y = F(x)$  in the grid provided.

$$F(1) = \quad F(3) = \quad F(4) = \quad F(6) =$$



$y = F(x)$

3. A drag racer accelerates at  $a(t) = (20 + t)$  ft/sec<sup>2</sup>.
- (a) How fast is the car traveling after 6 seconds? (The car is initially at rest.)
  - (b) How far has the car traveled after 6 seconds?
4. Find the integrals. Use the indicated method to get started.
- (a)  $\int_1^4 \frac{\sqrt{1 + \sqrt{x}}}{\sqrt{x}} dx$  (Substitution)
  - (b)  $\int t \sec^2 t dt$  (Integrate by parts)
5. Compute the integrals
- (a)  $\int \frac{dx}{(4 - x^2)^{3/2}}$
  - (b)  $\int \frac{dx}{x^2 + 4x + 8}$
6. Find the indefinite integral  $\int \frac{x^2 + 1}{x(x + 2)(x - 1)} dx$
7. Compute any **two** of the following; clearly mark your choices and indicate the method of integration.
- (i)  $\int \frac{1}{\sqrt{1 - x^4}} dx$
  - (ii)  $\int \frac{x}{\sqrt{1 - x^4}} dx$
  - (iii)  $\int \frac{x^2}{\sqrt{1 - x^4}} dx$
  - (iv)  $\int \frac{x^3}{\sqrt{1 - x^4}} dx$